Interference and Diffraction

Introduction

In the past two labs we've been thinking of light as a particle that reflects off of a surface or refracts into a medium. Now we are going to talk about light as a wave.

If you take two waves and add them together, or superimpose them, they will combine together to form a new wave. Below, in Figure 1, you see two different cases in which two waves a can add together.

In case 1a, the two waves are in phase, which means that they both reach a peak (or valley) at the same time. When these waves are combined the result will give you constructive interference.

In case 1b, the two waves are out of phase in such a way that peaks match with valleys. When these waves are combined the result will give you destructive interference.

If these are waves of light then we could say that constructive interference would give us a brighter light. For light waves that give us destructive interference, we would get darkness.
Double Slit Diffraction

Let's say that we have a situation in which laser light is incident on two very small slits. The slits are a distance, $d$, apart and a screen is placed a distance, $L$, from the slits. See Figure 2. Light from a laser is monochromatic, meaning it is made up of light with one wavelength. We use this single wavelength light so that we can simplify the analysis of the interference effects. If we shine a laser on the slits, the light waves will travel through each slit and then proceed to the screen. For points on the screen that are off of the central axis, one wave of light will travel a farther distance than the other.

If the two waves of light are in phase when they meet at the screen then you will see a bright spot (constructive interference).

If the two beams of light are out of phase when they meet then you will see a dark spot (destructive interference). As a result, you should see on the screen a pattern of bright and dark spots (or fringes). This pattern is shown as peaks of brightness and valleys of darkness in Figure 2.

\[
y = \frac{m \lambda L}{d}
\]

The location of the bright fringes can be found using the following equation.

In the lab you will be measuring the distance, $Y$, from one bright fringe to its counterpart fringe on the other side of the central axis. See Figure 2. You will then divide this distance by two, $y = Y/2$, and use this value in the above equation. This process will give you more accurate data.
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Single Slit Diffraction
There is also an interference effect when there is only one slit. This is called *diffraction*. In this situation the light interferes with itself to produce bright and dark fringes on the screen. The main difference in the pattern is that the central bright spot for one slit is twice as wide as the central bright spot for two slits. See Figure 3. There are other differences but they will be left for you to discover during the lab. Also the width of the slit is \( a \).

NOTE: This is not the distance between the slits, like for two slits. For diffraction you will be using the dark fringes as reference points when you are taking data.

\[
y = \frac{m\lambda L}{a}
\]

The equation for the locations of the dark fringes is given below.

Notice that the two equations are pretty much the same except for the \( d \) in one denominator and the \( a \) in the other. Also, one equation is for locating bright fringes due to *interference* with two slits. The other is for dark fringes due to *diffraction* with a *single slit*. You will be using these two equations to calculate the wavelength of the light from the laser. You will then compare this value to the known value of the wavelength.
The Equipment
You will be using the same optical bench set-up that you used last week. See Figure 4. In this lab however you will be using a laser as the light source. **Do not shine the laser into your lab partner's eyes!** There should be paper on your table for you to attach to the screen with a black clip. **Do not write on the screen!**

![Optical bench and accessories](image)

**FIGURE 4: Optical bench and accessories**

<table>
<thead>
<tr>
<th>Table 1: Data Table</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single Slit</td>
</tr>
<tr>
<td>L=m</td>
</tr>
<tr>
<td>a=a</td>
</tr>
<tr>
<td>m</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>...</td>
</tr>
<tr>
<td>6</td>
</tr>
<tr>
<td>%Error</td>
</tr>
</tbody>
</table>

**What you need to do:**

**Part 1 - Single Slit**

Place the Single Slit Disc on the optical bench. It should be about 3 or 4 cm from the laser. Rotate the disc so that the **0.08mm** (use **0.088mm** for calculations) slit is in the path of the laser beam. The screen should be at **110cm**. Using the black clip on the screen, attach the piece of paper to the screen. Adjust the laser to the left or the right so as to get as bright and sharp a pattern as possible on the screen. Make a copy of Table 1 in your lab report.

"m" should range from **1 to 6**. Now do the following ...

**A.)** Write on the piece of paper, "Single Slit, a = 0.088mm". Also place the value in your table.

**B.)** Measure the distance, L, from the **SLIT** to the screen. (*Not from the laser*)

**NOTE:** The disc is not even with marker at the base of the mount.
C.) Using the 1st through the 6th order dark fringes, make marks at the estimated centers of the dark fringes.

D.) Label on the paper the order number for each pair of fringes.

E.) Remove the paper and put up a new piece of paper. DO NOT USE THE SAME SHEET! You'll use this for the double slit.

Using your marked pattern, do the following for each fringe pair ...

F.) Measure the distance, Y, from one dark fringe to the other for the same order number. See Figure 3. Place these values in the table.

G.) Calculate the distance, y, which is the distance from the center of the central maximum to a dark fringe. Place these values in the table.

H.) Using the Single Slit - Dark Fringe equation, calculate the wavelength for each order. (Make sure all of the values are in meters before you substitute in the numbers.) Place these values in the table.

I.) Find the average of your 6 wavelengths.

J.) Calculate a percent error based on the known wavelength for the green laser light, 532nm, or red laser light, 650 nm.

Question #1 Turn the disc to the Variable Slit section. Rotate the disc while the laser is centered on the variable slit. Describe what happens to the pattern as the slit width increases. Does this agree with the \( y = \frac{m \lambda L}{a} \) equation? Explain.

Question #2 Turn the disc so that the laser is shining on one of the following three patterns: squares, hexes, holes.
   a. For each pattern, describe or diagram what you are seeing.
   b. Based on what you have seen in the first part of the lab, explain why the patterns look the way they do for each type of "slit".
Part 2 - Double Slit

Place the Multiple Slit Disc on the optical bench. It should be about 3 or 4cm from the laser. Shine the laser where \( d = 0.25 \text{mm} \), this slit is in the Double Slit section where it says \( a = 0.04 \), \( d = 0.25 \). Make another copy of the table, but now it will be Double Slit and the "a" becomes a "d". Now do the following ...

A.) Write on the piece of paper, "Double Slit, \( d = 0.25 \text{mm} \). Also place the value in your table.

B.) Measure the distance, \( L \), from the slit to the screen.

C.) Using the 1\(^{st}\) through the 6\(^{th}\) order \textbf{bright} fringes, make marks at the estimated centers of the bright fringes.

D.) Label on the paper the order number for each pair of fringes.

Using your marked pattern, do the following for each fringe pair ...

E.) Measure the distance, \( Y \), from one bright fringe to the other for the same order number. See \textbf{Figure 2}. Place these values in the table.

F.) Calculate the distance, \( y \), which is the distance from the center of the central maximum to a bright fringe. Place these values in the table.

G.) Using the Double Slit - Bright Fringe equation, calculate the wavelength for each order. (Make sure all the values are in \textbf{meters} before you substitute in the numbers). Place these values in the table.

H.) Find the average of your 6 wavelengths.

I.) Calculate a percent error based on the known wavelength for the green laser light, 532 nm, or the red laser light, 650nm.

**Question #3** Turn the disc to the Variable Double Slit. Rotate the disc while the laser is centered on the variable slit. Describe what happens to the pattern as the slit separation increases.

Does this agree with the \( y = \frac{m\lambda L}{d} \) equation? Explain.

**Question #4** While rotating the disc for question three note that while the slit separation was changing, the slit width was constant, what do you observe about the projection that reflects that the slit width was constant?
CD and DVDs

For this part of the experiment we will use the grooves on a CD for multiple slit interference. As shown on the right the actual slits we are working with are the lines of indents. For standard cases one side of the CD or DVD has a reflective material, but if we remove the reflective material we can use the clear disk for multiple slit transmission. Keep in mind the area the laser will be shining on is much, much larger than that pictured here, approximately 1000 times so.

The setup you will use is shown below. Be sure to note the location of the laser is such so that it is hitting the groove where it is approximately vertical.
You’ll also find pictures of the setup on the following page.
Figure 1: Picture of CD setup

Figure 2: Picture of CD setup
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Calculations:
Now calculate $\vartheta$ and $d$ (The groove spacing) using values you can measure here.

A.) As with the double slit experiment measure the distance between bright fringes to find $y$ and divide by two to find $y$. Be sure you’re measuring from $m=1$ to $m=1$, do not measure from the center point.

B.) Measure $L$, the distance from the cardboard screen to the CD, refer to the diagram on page 7.

C.) Calculate $\vartheta$ using $y$ and $L$ and trigonometry.  
*Hint: Refer to the diagram on page 7 and use either $\sin \vartheta$ or $\tan \vartheta$.*

D.) Use the formula for diffraction, *(remember this one, we’ll be using it quite often this semester)*

$$d \sin \vartheta = m \lambda$$

to solve for the groove spacing $d$ (a.k.a. track pitch). For your calculation here use the given lambda for the green or red laser light of 532nm, or 650nm and the theta you calculated in C.

E.) Calculate a percent error between this value and the given value for track pitch in the table on the next page.

F.) Now repeat A,B,C,D, and E using either a transparent or reflective DVD. You should now have the track pitch for both CD and DVD.

G.) Optionally repeat F.) for the Blu-ray if you’re interested.

**Question 5:**

a.) How do the track pitches ($d$ values) of the CD and DVD compare? (shorter/longer etc.)

b.) Does this correspond with what you know about the amount of information on each respective disk? Explain your answer

**Question 6:**

To get a feel for the size of these grooves compare this distance $d$ to the size of the average human red blood cell of 10 $\mu$m. Are they smaller, larger, about the same?
Appendix:
What is the track pitch or groove spacing on a CD DVD or Blu-ray?

Answer: The groove spacing is also called the "track pitch". It is the distance between each track. Below is a list of the track pitches of some common formats.

<table>
<thead>
<tr>
<th>Type</th>
<th>Capacity</th>
<th>Track pitch</th>
<th>Wavelength of laser light</th>
<th>Numerical Aperture</th>
</tr>
</thead>
<tbody>
<tr>
<td>CD</td>
<td>0.7Gb</td>
<td>1.60 ±0.1 µm</td>
<td>780nm</td>
<td>0.45</td>
</tr>
<tr>
<td>DVD</td>
<td>4.7Gb</td>
<td>0.74 µm</td>
<td>650nm</td>
<td>0.60</td>
</tr>
<tr>
<td>Blue-ray</td>
<td>25 Gb</td>
<td>0.32 µm</td>
<td>405nm</td>
<td>0.85</td>
</tr>
</tbody>
</table>

Because of diffraction they can't make the 'grooves' to close together. (Diffraction is the reason you see a play of colors on CDs and DVDs.) Notice the shorter the wavelength of the laser light they use the closer they can make the grooves and the more information they can get on the disk. Also notice however that the track pitch decreases more rapidly than the wavelength of the lasers in the above table, this is because you can also reduce the track pitch if you increase what is called the Numerical aperture of the lens you use. In fact how much information you can store on a disk depends on how small you can get the "spot size" of the laser beam and the radius of the smallest spot that you can get equals the laser light wavelength divided by the numerical aperture. (R=NA)

(1 µm = 1 micrometer = 1 micron = 0.000001 meters = 1x10^-6 meters) (1 nm = 1 nanometer = 1x10^-9 meters)